

## Pupil worksheet

### Planets outside our Solar System

Scientists have detected more than 1800 exoplanets, the planets that orbit stars beyond our Sun. Many more await discovery.

How do we find an exoplanet? What can we learn about its orbit, its mass and its temperature? Might life exist on its surface? This activity is your chance to find out.

### Detecting exoplanets

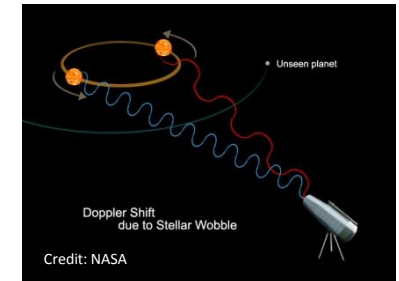
You cannot look through an ordinary telescope and see an exoplanet. Its reflected light is difficult to see next to the dazzling brightness of its star. Instead, scientists use methods like these:

- The **transit method**, in which a telescope detects a periodic dip in the brightness of a star every time an orbiting planet passes between the star and the telescope.
- **Direct imaging**, in which a masking device is attached to an Earth- or Space-based telescope to block out light from the star. This makes objects around it, including planets, easier to see.
- The **radial velocity or Doppler method**, also called the **wobble method**. The method makes use of the difference between the frequency of a wave emitted and that of the wave received when there is relative movement of the wave source and the observer. This technique was used in the earliest exoplanet discoveries. Read on to find out how it works.

### The Doppler method

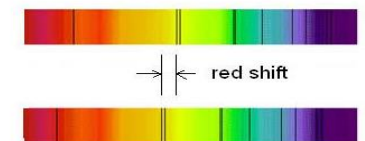
The composition of every star is unique, so each star has its own absorption spectrum. The black lines in an absorption spectrum show the frequencies of light absorbed by the elements in the cooler, gaseous surface layers of the star.

As a planet orbits its star, gravitational forces pull the objects towards each other. As the planet orbits the star, the star also moves in a smaller orbit around the centre of mass of the system. This causes variations in the **radial velocity** of the star. Radial velocity is the speed at which a star moves towards or away from us.



As the planet moves in its orbit away from us, the star moves towards us. This compresses its light waves slightly, so the absorption lines move towards the blue end of the spectrum. This is **blueshifting**.

As the planet moves towards us, the star moves away. The light waves that the star emits spread out, so the absorption lines move towards the red end of the spectrum. This is **redshifting**.



You can use the expression below to estimate the radial velocity  $v$  of a star:

$$\frac{\Delta\lambda}{\lambda} \approx \frac{v}{c}$$

In the expression,  $\lambda$  is the emitted wavelength and  $\Delta\lambda$  is the change in wavelength from Doppler shift. The value of  $c$ , the speed of light, is  $3 \times 10^8$  m/s.

### What to do

Watch the animation showing the Doppler method for finding exoplanets:

## Key Stage 5 – Exoplanet estimator

### 51 Pegasi b

51 Pegasi b was one of the first exoplanets to be discovered, in 1995. It was found using the Doppler method. It is the only planet known to be orbiting its star, 51 Pegasi. The star is a Sun-like star. It is about 51 light years from earth in the constellation Pegasus.

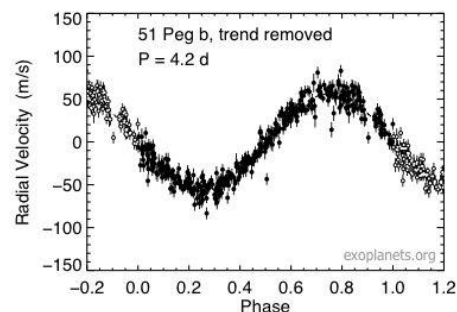
Your task is to estimate the radial velocity and orbital period of the planet and the distance from its star. You will also estimate its mass.

#### Step 1 – Radial velocity

One of the absorption lines on the spectrum for the star has  $\lambda = 656.300000$  nm. This shifts to 656.300123 nm when the star is moving away from the observer.

a Use the expression  $\frac{\Delta\lambda}{\lambda} \approx \frac{v}{c}$  to estimate a value for the maximum radial velocity  $v$  of the star, 51 Pegasi. Give your answer in m/s.

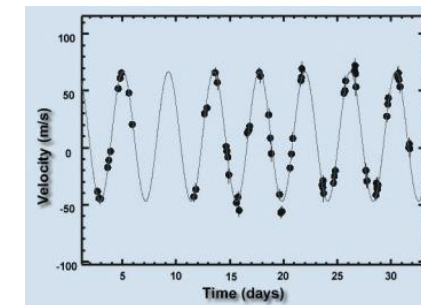
b The graph shows the change in radial velocity over time for 51 Pegasi. Compare your estimated value for the maximum radial velocity to that shown on the graph. How similar are your values?



#### Step 2 – Orbital period

This graph is similar to the previous one, but it shows the radial velocity trend line.

Use the graph to estimate the time between consecutive maxima. This is the time taken by the planet to orbit its star, or its **orbital period, T**.



Graph: adapted from Marcy and Butler

#### Step 3 – Distance from star to planet

Kepler's third law links the orbital period of a planet,  $T$ , to the distance from its star,  $r$ . The equation is:

$$T^2 / r^3 = 4\pi^2 / G M_*$$

Where  $G$  is the universal gravitational constant and  $M_*$  is the mass of the star.

Use the equation to estimate the value of  $r$ , the distance from the planet to its star, using SI units. The mass of the star, 51 Pegasi, is  $2.2 \times 10^{30}$  kg.  $G$  is the Gravitational Constant. Its value is  $6.674 \times 10^{-11} \text{ m}^3 \text{ kg}^{-1} \text{ s}^{-2}$ .

#### Step 4 – Speed of planet

Now estimate the speed that the planet, 51 Pegasi b, is moving. Use the equation  $speed = \frac{distance}{time}$

The distance is how far the planet travels in one complete orbit. Assuming a

Graph: James McBride

circular orbit, distance =  $2\pi r$ . The time is its orbital period,  $T$ .

## Key Stage 5 – Exoplanet estimator

### 51 Pegasi b (continued)

#### Step 5 – Mass of planet

We might say that the planet 51 Pegasi-b is orbiting its star. However, it is actually orbiting the centre of mass of the star-planet system.

The two objects have the same orbital period, so the centre of mass does not move and the system does not experience a change in momentum. This means that the planet and the star have equal magnitudes of momentum. Since momentum is equal to the product of mass and velocity:

$$M_* v_* = M_{planet} v_{planet}$$

- Use the equation above the values below to estimate  $M_{planet}$ 
  - your value of  $v_{planet}$  (the speed that the planet is moving) from step 4
  - $M_*$  (given in step 3)
  - $v_*$  (the radial velocity of the star, calculated in step 1)
- Your value is an estimate of the minimum mass of the planet. Explain why the value cannot be accurate.

#### Step 6 – Comparing the planet to those in our Solar System

[www.oxfordsparks.net/planet](http://www.oxfordsparks.net/planet)

Use the data in the table on the right to compare 51 Pegasi b to some of the planets in our own Solar System.

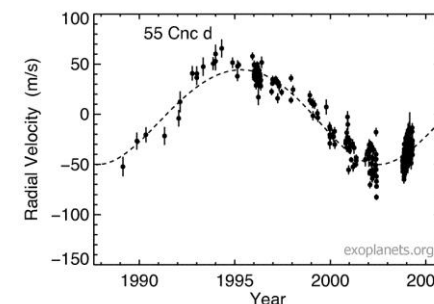
Do you think the planet might be habitable (support life)? Explain your decision.

Planet	Distance from star (km)	Orbital period (Earth days)	Mass of planet (kg)	Average surface temperature (K)
Mercury	$58 \times 10^6$	88	$330 \times 10^{21}$	440
Earth	$150 \times 10^6$	365	$6.0 \times 10^{24}$	288
Jupiter	$780 \times 10^6$	4332	$1.9 \times 10^{27}$	165
51 Pegasi b				1265

### An extra exoplanet

#### 55 Cancri d

55 Cancri d is one of five planets that orbits the star 55 Cancri A. The graph shows how the radial velocity of the star changes over time as a result of the orbit of 55 Cancri d.



Graph: James McBride

- From the graph, estimate the orbital period of the planet.
- Select and use an equation to estimate the distance of the planet from its star. The mass of the star is  $1.89 \times 10^{30}$  kg.
- Estimate the speed at which 55 Cancri d is moving. Then use data from the table to estimate the speed at which Earth is moving. Compare the two values.

- d** Compare the data for 55 Cancri d to the data for the planets in the table above. Its estimated minimum mass is  $7.2 \times 10^{27}$ .
- e** Do you think the planet might be habitable? Explain your decision. What extra information might help you to decide? Can you use the Internet to find out any of this information?